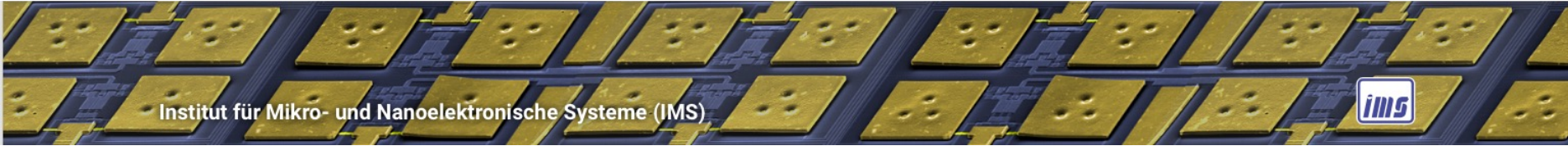
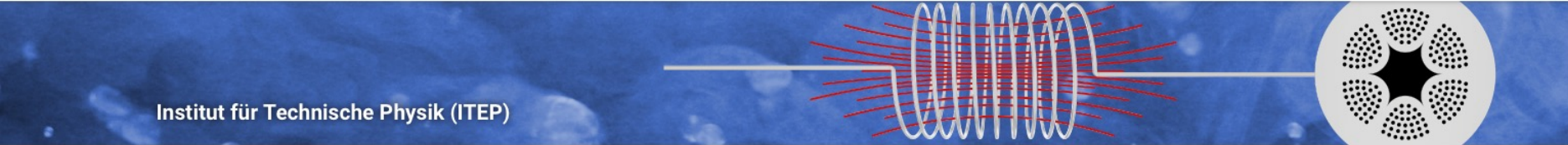


Superconductivity for Engineers

Prof. Dr. Sebastian Kempf, Prof. Dr. Bernhard Holzapfel
Summer term 2021



Institut für Mikro- und Nanoelektronische Systeme (IMS)



Institut für Technische Physik (ITEP)



(Preliminary) Schedule

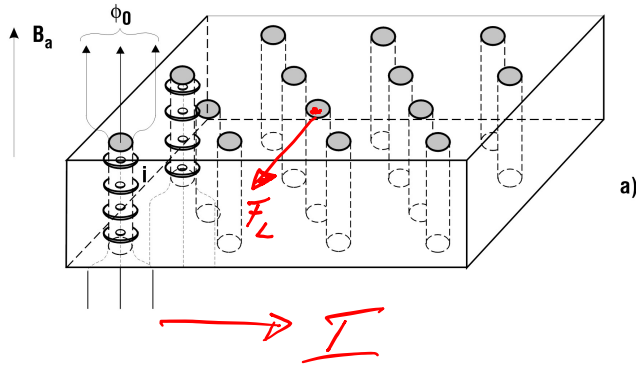
	Day	Date	Lecture / Tutorial	Day	Date	Lecture / Tutorial
1	Mon	21-04-12	Lecture 1 (SK)	Wed	21-04-14	
2	Mon	21-04-19	Lecture 2 (BH)	Wed	21-04-21	
3	Mon	21-04-26	Lecture 3 (SK)	Wed	21-04-28	Tutorial 1 (IMS)
4	Mon	21-05-03	Lecture 4 (SK)	Wed	21-05-05	
5	Mon	21-05-10	Lecture 5 (SK)	Wed	21-05-12	Tutorial 2 (IMS)
6	Mon	21-05-17	Lecture 6 (SK)	Wed	21-05-19	Tutorial 2 (IMS)
7	Mon	21-05-24	---	Wed	21-05-26	
8	Mon	21-05-31	Lecture 7 (BH)	Wed	21-06-02	Tutorial 3 (IMS)
9	Mon	21-06-07	Lecture 8 (BH)	Wed	21-06-09	Tutorial 4 (ITEP)
10	Mon	21-06-14	Lecture 9 (BH)	Wed	21-06-16	
11	Mon	21-06-21	Lecture 10 (BH)	Wed	21-06-23	Tutorial 5 (ITEP)
12	Mon	21-06-28	Lecture 11 (BH)	Wed	21-06-30	
13	Mon	21-07-05	Lecture 12 (BH)	Wed	21-07-07	Tutorial 6 (ITEP)
14	Mon	21-07-12	Lecture 13 (SK)	Wed	21-07-14	
15	Mon	21-07-19	Lecture 14 (SK)	Wed	21-07-21	Tutorial 7 (IMS, ITEP)

(Preliminary) Lecture content

- Lecture 1: (SK) Introduction and overview
- Lecture 2: (BH) Superconductor applications
- Lecture 3: (SK) Normal metals and properties of the normal conducting state
- Lecture 4: (SK) Perfect conductor, ideal diamagnetism, Two-Fluid-Model, London theory
- Lecture 5: (SK) Disordered superconductors, Pippard theory, microwave properties
- Lecture 6: (SK) BCS theory
- Lecture 7: (BH) Type-II superconductors, Current transport**
- Lecture 8: (BH) Bean Model, Ginzburg-Landau theory**
- Lecture 9: (BH) Type-I superconductors**
- Lecture 10: (BH) Type-II superconductors**
- Lecture 11: (BH) Pinning and superconducting permanent magnets**
- Lecture 12: (BH) ac-losses, electrical stabilization and thermal aspects**
- Lecture 13: (SK) Josephson junctions and SQUIDs
- Lecture 14: (SK) Josephson junctions and SQUIDs

Current transport in ideal type II superconductors

Shubnikov phase



→ Ideal SC = without defects

→ Lorentz force $\vec{F}_L = \vec{j} \times \vec{B}$ acts on FL

↳ FL will move

↳ dissipation of energy by R

→ $N_c J_c$

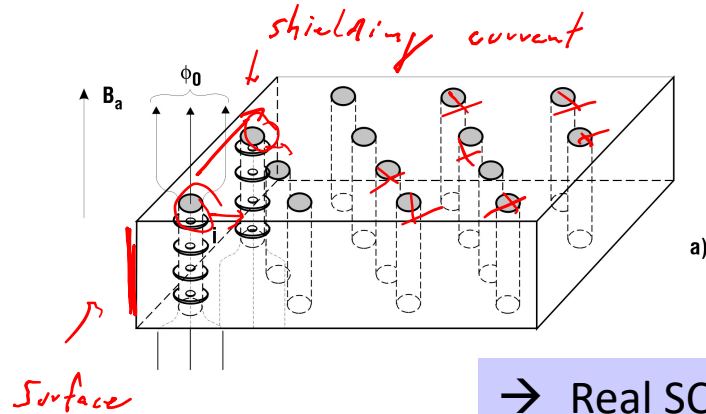
→ Need to pin FL

No dissipation free current transport in ideal type II superconductors in the Shubnikov Phase !!!

Current transport in real type II superconductors

↳ with defects

Shubnikov phase

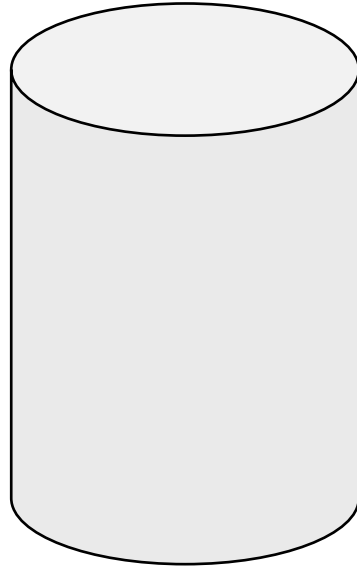


- Real SC = SC with defects
- Flux pinning at defects
- Flux lines move only if current induced Lorentz Force $F_L > F_p$
- $J_c > 0$
- Inhomogeneous flux distribution inside SC

Flux distribution in real type II superconductors

The Bean Model

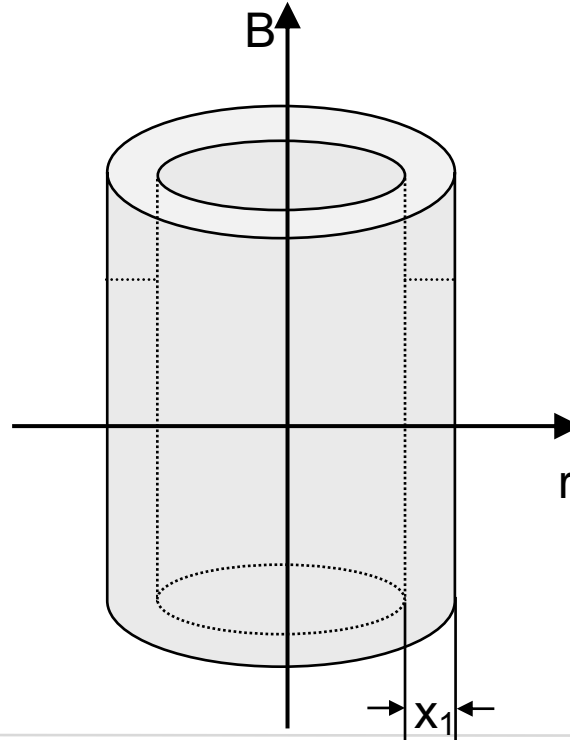
$$B_a = 0$$



Flux distribution in real type II superconductors

The Bean Model

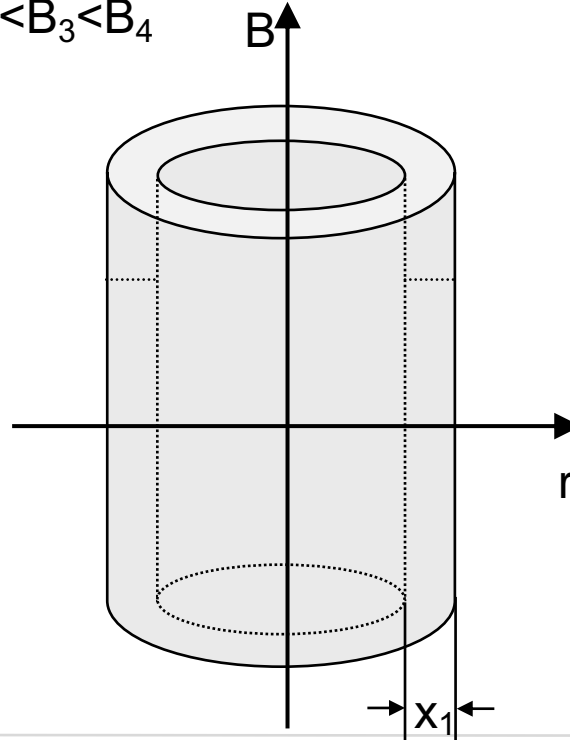
$$B = B_1$$



Flux distribution in real type II superconductors

The Bean Model

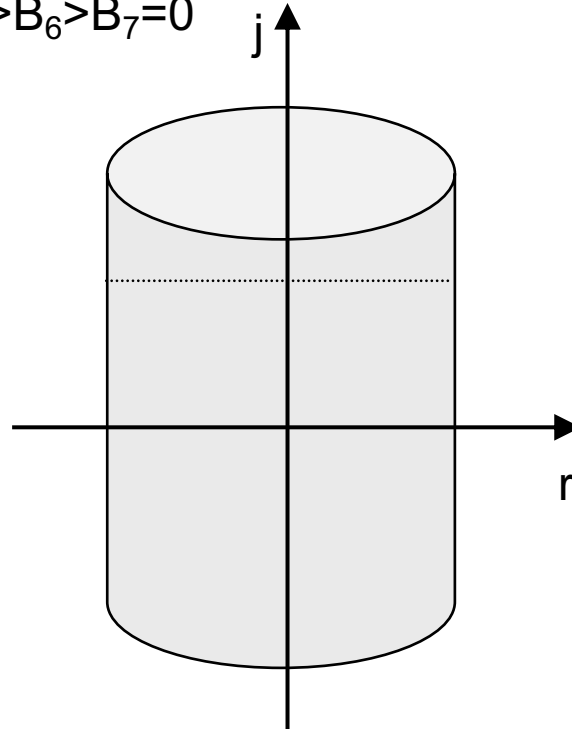
$$B = B_1 < B_2 < B_3 < B_4$$



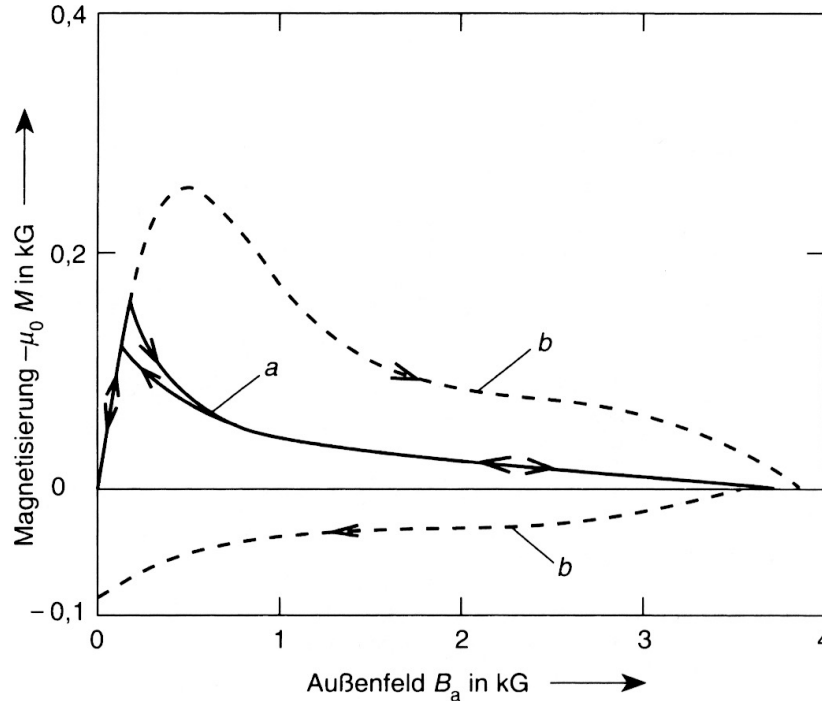
Flux distribution in real type II superconductors

The Bean Model

$$B = B_4 > B_5 > B_6 > B_7 = 0$$



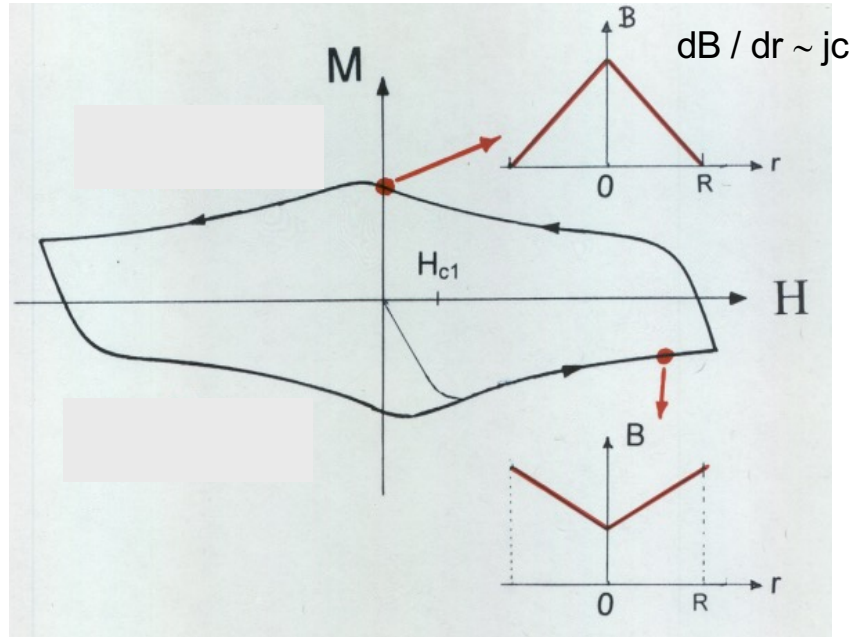
Magnetization of „real“ type II superconductors



- a) Annealed
- b) With defects

Hysteresis of type II superconductors

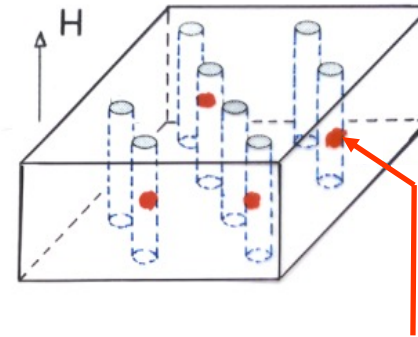
Magnetization and flux profile



$H > H_{c1} \Rightarrow$ flux penetration

$$\Phi_0 = 2 \cdot 10^{-15} \text{ Tm}^2$$

$$\xi = 1,8 \text{ nm}$$



Pinning of flux lines by defects (pinningcenter)

Ginzburg-Landau-Theory: General remarks

- **First published in russian**
V.L. Ginzburg and L.D. Landau, *Zh. Eksp. Teor. Fiz.* **20** (1950) 1064
- **Appreciated only gradually in the West**
- **Abrikosov predicted 1957 the flux line lattice based on GL**
- **Phenomenological theory, no need for microscopic understanding;**
but might be deduced from microscopic theories (from BCS theory by Gorkov in 59)
- **Also known as Ginzburg-Landau-Abrikosov-Gorkov (GLAG) theory**
- **Can deal with non-uniform superconducting states**
(Shubnikov phase - flux distribution; proximity effect; fluctuations)
- **Based on an earlier theory of Landau on phase transitions in general**

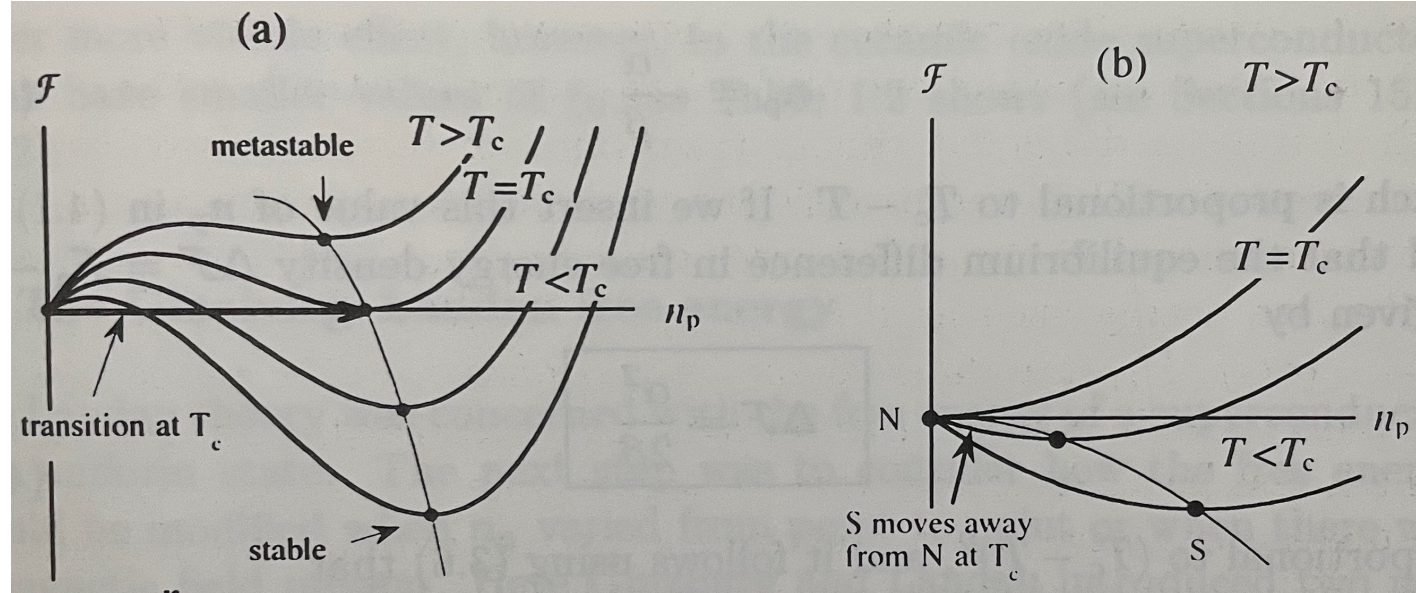
Landau-Theory of phase transitions

- Phase transition is characterized by the onset of an „order parameter“ during variation of temperature or other variables



- For superconductivity: macroscopic wave function is complex order parameter
- The relevant thermodynamic function depend on the order parameter and the form of this function determines the degree of the phase transition

Landau-Theory of phase transitions



Landau-Theory of phase transitions

- For a second order phase transition $\mathcal{F}(n_p, T)$ is analytic, shows a minimum at T_c and $n_p=0$ and can be expanded around this point in powers of n_p and $(T-T_c)$
- GLAG is valid around T_c !

$$\mathcal{F}(n_p, T) = \mathcal{F}_n(T) + \alpha(T)n_p + \frac{1}{2}\beta(T)n_p^2 + \dots$$

$$\Delta\mathcal{F} = \mathcal{F}_n - F_s = \frac{\alpha^2}{2\beta}$$

Minimum of $\mathcal{F}(n_p, T)$:

$$d\mathcal{F}/dn_p = 0 \rightarrow \alpha + \beta n_p = 0 \quad d.h. \quad n_p = -\frac{\alpha}{\beta}$$

$$B_c(T) = -\sqrt{\frac{\mu_0}{\beta}} \alpha(T)$$